

New Directions in Search-Based Structured Prediction: Multi-Task Learning and Integration of Deep Models

PhD Final Exam Presentation

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Introduction



<u>Search-Based</u> Structured Prediction:



Structured Prediction Frameworks



We can classify most of the structured prediction approaches into this four cell table.

	Non-Deep Models	Deep Models			
Non- Search- Based	CRFs, SSVM, SPerceptron	DSM, SPEN, DVN			
Search- Based	LaSO, PruneScore , HC-Search, MTSP	Seq2Seq-BSO HC-Nets			
•	This Thesis				

Partial vs. Complete Output Space





Contributions



- 1. Developed *Prune-and-Score* to improve the accuracy of greedy policy based structured prediction with large action spaces.
- 1. Studied three learning architectures for multi-task structured prediction (**MTSP**) problems with different trade-offs between speed and accuracy.
- 1. Proposed a *HC*-Nets framework that synergistically combines the advantages of output space search based structured prediction methods and deep models.



Prune-and-Score: Learning Greedy Policy for Structured Prediction

For some problem, even with greedy search, the branching factor is still too large to make the correct decision.

This work tries to answer following questions:

- Can we prune the action space at each step to reduce the branching factor and improve the accuracy?
- Can we formulate the imitation learning problem to an offline rank learning problem?

Coreference Resolution: The Problem



Extracted Mentions



Coreference Resolution: Problem Setup



[Ramallah ([West Bank])]10-15 ([AFP]) – [Eyewitnesses] reported that [Palestinians] demonstrated today Sunday in the [West Bank] against the [Sharm el-Sheikh] summit to be held in [Egypt] tomorrow Monday. In [Ramallah], [around 500 people] took to [the town]'s streets chanting slogans denouncing the summit ...





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Current mention: [Ramallah (West Bank)]





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Current mention: [Sharm el-Sheikh]







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Current mention: [Sharm el-Sheikh]







Successor Function



[Ramallah ([West Bank])]10-15 **([AFP]**) – **[Eyewitnesses]** reported that [Palestinians] demonstrated today Sunday in the **[West Bank]** against the [Sharm el-Sheikh] summit to be held in **[Egypt]** tomorrow Monday. In [Ramallah], **[around 500 people]** took to **[the town]**'s streets chanting slogans denouncing the summit ...





Successor Function



State: partial coreference output













Ore





Orea







Oregor



Prune-and-Score: Learning Approach

We optimize the overall loss of the Prune-and-Score approach in a *stage-wise* manner.

Stage 1: Learn pruning function to optimize the pruning error.

$$\hat{\mathcal{F}}_{prune} \approx \arg \min_{\mathcal{F}_{prune} \in \mathbf{F}_{\mathbf{P}}} \epsilon_{prune}$$

Stage 2: Learn scoring function conditioned on the learned pruning function.

$$\hat{\mathcal{F}}_{score} \approx \arg \min_{\mathcal{F}_{score} \in \mathbf{F}_{s}} \epsilon_{score} \hat{\mathcal{F}}_{prune}$$

conditioned

Experimental Setup



Datasets

 MUC 6: Message Understanding Conference (MUC6, 1995) Train/Dev/Test: 268/68/107 documents
ACE 2004: Automatic Content Extraction (NIST, 2004) Train/Dev/Test: 195/30/30 documents

Evaluation Metrics

MUC F1, BCubed F1, CEAF F1.

Base Ranker Learner

LambdaMART (Burges, 2010), implemented in RankLib

Baseline Approaches

Only Scoring Function UIUC: CPL³M (Chang et al., 2013) JHU: Easyfirst (Stoyanov and Eisner, 2012) Stanford: Multi-Sieves (Raghunathan et al., 2010)



Prune-and-Score vs. State-of-the-Art

	ACE 2004			MUC 6		
F-1 score	MUC	B-Cubed	CEAF	MUC	B-Cubed	CEAF
Prune-Score	78.6	83.04	79.42	85.27	80.49	67.83
Only Scoring	75.4	80.75	78.58	83.76	77.11	64.91
JHU	80.1	81.8	-	88.2	77.5	-
UIUC	78.29	82.2	79.26	-	-	-



Summary of Prune-and-Score

- h Coreference Resolution as a greedy search process
- h Key Idea: Scoring Function Pruning Function + Scoring Function
- h Apply the offline rank learner for imitation learning
- h Achieved results that are comparable than the state-of-the-art



Multi-Task Structured Prediction (MTSP) for Entity Analysis

What if you want to solve multiple corelated structured prediction tasks with complete output space search?

We can concatenate the output of multiple tasks to form a super-output. But search on such super-output would be slow due to the huge branching factor.

We want to use complete output space so that we can extract high-order features to exploit the interdependencies between tasks

• Can we do complete output space search for multiple tasks accurately and efficiently?

Example of NLP Pipelines





A composite NLP system for Text Comprehension and Question Answering

Entity Analysis Tasks



The NLP tasks that are related to "entity mentions"



Problem Setup



i=1 i=2

He left [**Columbia**] in 1983 with a BA degree, ... after graduating from [**Columbia University**], he worked as a community organizer in Chicago...
Problem Setup





Left-linking Tree formulation for coreference resolution:



Problem Setup





Problem Setup





Multi-Task Structure Prediction



Multi-Task Structured Prediction (MTSP):



• How to exploit the interdependencies between tasks?

Multi-Task Structure Prediction



Introduce Inter-task Features:







Learning k (= 3) independent models, one after another;



Define a order: Task 1 → Task 2 → Task 3



Learning k (= 3) independent models, one after another;





Learning k (= 3) independent models, one after another;











Joint Architecture

Task 1 & 2 & 3:



 $\phi = \phi_1(x,y) \circ \phi_2(x,y) \circ \phi_3(x,y) \circ \phi_{(1,2)}(x,y,y') \circ \phi_{(1,3)}(x,y,y'') \circ \phi_{(2,3)}(x,y',y'')$ Vector concatenation



Pipeline architecture



Connect the tail of pipeline to the head?



Unshared-Weight-Cyclic Training

- Step 1: Define a order: Task 1 → Task 2 → Task 3
- Step 2: Predict initial outputs:





Step 1: Define a order: Task $1 \rightarrow$ Task $2 \rightarrow$ Task 3

Y1

Y2

V3

Step 2: Predict initial outputs:







- **Step 1:** Define a order: Task $1 \rightarrow$ Task $2 \rightarrow$ Task 3
- Step 2: Predict initial outputs:











- **Step 1:** Define a order: Task $1 \rightarrow$ Task $2 \rightarrow$ Task 3
- Step 2: Predict initial outputs: y_1



 V_2

V3



All metrics are accuracies (larger is better)

Results Cyclic Architecture Performance



ACE05 Test Set Performance TAC15 Test Set Performance Train Within. Cross. Coreference Link NER NER Link NERLC Train. Algms. time Coref Coref Accu. MUC BCube CEAFe CoNLL Accu. Accu. Algm. Accu. **CONLL CEAFm** Accu. time Berkeley 81.41 74.7 72.93 76.35 85.6 76.78 31min Rank-1st 87 73.7 80 a. Results of Joint Architecture without Pruning Berkelev 88.9 74.8 82.98 80.8 6m29s 72.8 **STSP** 80.28 73.26 71.58 75.04 82.24 a. Results of Joint Architecture without Pruning 75.36 **9**min STSP 87.3 76.2 Joint w. 70.9 81.21 78.8 2m41s 80.23 73.79 72.03 75.35 82.20 76.99 48min Rand Init Joint w. 71.17 68.33 81.31 87.1 78.4 7m19s Rand. Ini Joint w. 82.18 76.57 74.00 77.58 85.71 78.77 34min Good init Joint w. 89.72 76.98 82.8 74.43 81.3 6m11s b. Results of Joint Architecture with Pruning Good. Ini b. Results of Joint Architecture with Pruning Score-81.10 75.79 74.33 77.07 85.63 78.71 16min agnostic Score-89.54 76.84 74.31 82.99 81.4 4m15s Scoreagnostic 82.81 75.77 74.96 77.85 87.18 80.28 **37**min sensitive Score-89.33 77.68 74.63 83.17 81.3 9m2s c. Results of Cyclic Architecture sensitive c. Results of cyclic Architecture Unshrd-81.83 76.05 73.99 77.29 84.18 80.67 11min Wt-Cyclic Ushrd-74.6 89.57 77.68 82.08 80.5 3m52s Wt-Cvc

Competitive accuracy, and much faster training

Summary of MTSP for Entity Linking



- 1. Formulated the problem of multi-task structured prediction (MTSP) in the context of entity analysis of NLP.
- 1. Developed a search-based learning framework: structured SVM for training; beam search for inference.
- 1. Studied three architectures: *pipeline, joint*, and *cyclic* to trade-off between accuracy and speed.
- 1. Evaluated two pruning approaches for the joint architecture

HC-Nets: A Framework for Search-based Deep Structured Prediction



Prior search-based structured prediction approaches use hand-coded features.

We develop a general search-based framework that can perform **neural network function** learning under the **discrete complete output space**.

The decomposition of heuristic and cost functions makes the representation more expressive and learning more modular.

HC-Nets for Structured Prediction







Input *x*

Search State

 y_0

Initial State

Starting point of search


































Search Space Design





Search Space Design





Continuous representation vs Discrete

representation? Continious representation: richer input information **Discrete representation**: (a) no need rounding threshold; (b) easy to define hard constraints.

Search Space Design



We will apply *k-Flipbit* search space, an extension of standard Flipbit space.







Initial

State.

- Use random initial states to avoid the overfitting for a particular initial state.
- Use learned initial states, where we use a learned I.I.D. classifier to predict each output bit independently. (e.g., Logistic Regressor)

Terminal

State.

- Complete output space search have no hard criteria of terminal state.
- A common condition to stop: reaching a locally optimal state or reaching the maximum depth limit.

H and *C* networks are usually <u>task-specific</u>.

 $f\colon X\times Y \to R^+$

Input: the input-output presentation pair **Output**: a real-value score

Stage-wise Learning for *H* **and** *C*



Heuristic Function Training

Goal: **Uncover** a set of candidate "high quality" outputs.



Cost Function Training

Goal: Optimize over the best cost output among candidate set.

$$\hat{y} \xleftarrow{} \min_{y \in S} C(x, y)$$
Update: new $\theta_C \xleftarrow{} \min_{\theta_C} \sum_{error(x, \hat{y}, y^*)} Error(x, \hat{y}, y^*)$

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Heuristic Function Learning



Key steps:

1. For each input, run search guided by true loss function (e.g., F1)



Heuristic Function Learning



Key steps:

1. For each input, run search guided by true loss function (e.g., F1)



2. Aggregate the uncovered states during search into a set R



Heuristic Function Learning Key steps:



- ncy steps.
 - 1. For each input, run search guided by true loss function (e.g., F1)



2. Aggregate the uncovered states during search into a set R



3. After reaching mini-batch examples, sent R into optimizer to do weight update, then clear R



Blackbox Optimizer Reductions







Ranking Based Learner



Learning a ranker given ranking constraints.

For input $oldsymbol{X}$



Ranking Based Learner





Reduction Summary



Drawbacks of regression-based learning

- First, only the **relative relations** are needed.
- Second, the internal relations of sibling states were not exploited.

Drawbacks of ranking-based learning

• Training is very computational expensive.

Experimental Setup



Multi-label Classification

- We would evaluate on three datasets: *Bibtex*, *Bookmarks* and *Yeast*.
- We will report F1 accuracy.



Our H or C network is derived from SPEN and DVN

Experimental Setup



Multi-label Classification

- Maximum number of epoch = 300.
- Randomly split out 5% of the examples as validation set.
- Learning rate, 0.005 for Yeast, and 0.1 for the other three.
- We use the gradient descent optimizer to perform the weight update.





Image Segmentation

Evaluate on *Weizmann Horse* Dataset. Label Set: {Background = 0, Horse = 1} Use *Intersection-of-Union (IoU)* and *Pixelwise-Accuracy* to evaluate the result.



Our cost function network is derived from DVN

Experimental Setup



Word Recognition

We use a synthetic word recognition dataset, constructed from *Char74k* by taking a list of 50 common five-letter English words.



Evaluate with character-wise Hamming accuracy.

Results



Accuracy comparison with HC-Nets and the other SOTA approaches.

		Multi-Lab	el	Word Recog. Image Segn	
Algorithms	Yeast	Bibtex	Bookmarks	HW-Words	Horse32x32
		F-1		Char Acc.	IoU
SPEN(E2E)	63.8	38.1	33.9	42.26	75.45
DVN	63.8	44.7	37.1	-	84
InfNet	-	42.2	37.6	37.95	69.31
NLStruct	-	-	-	44.37	81.86
Rand-Init	62.5	43.2	34.9	39.02	74.62
Learned-Init	62.6	44.7	37.8	45.14	82.55

Results



• Analysis of the varying the maximum search depth of generation stage.

HL-Search

• We present the generation and selection accuracy with 2 initialization methods.

Depth	Gen.Acc.		RealAcc.			Depth	Gen.Acc.		RealAcc.		
	Rand-Init	Learned- Init	Rand-Init	Learned- Init			Rand-Init	Learned- Init	Rand-Init	Learned- Init	
Yeast						Words Recognition					
2	0.531	0.674	0.462	0.579		1	0.22	0.41	0.15	0.28	
5	0.755	0.816	0.553	0.623		5	0.56	0.67	0.32	0.35	
10	0.816	0.831	0.564	0.627		10	0.74	0.88	0.38	0.41	
14	0.854	0.841	0.598	0.629		15	0.83	0.91	0.37	0.404	
	Bibtex					Horse32x32					
2	0.698	0.722	0.312	0.375		10	0.24	0.68	0.164	0.531	
3	0.722	0.748	0.384	0.421		20	0.57	0.73	0.415	0.628	
4	0.759	0.801	0.385	0.425		50	0.79	0.86	0.614	0.719	
5	0.762	0.811	0.385	0.426		65	0.88	0.93	0.628	0.698	
Bookmarks											
2	0.791	0.84	0.285	0.344							
3	0.791	0.856	0.279	0.357							
4	0.792	0.882	0.292	0.358							

Future Work



1. End-to-End MTSP with Deep Neural Networks.

How to formulate the problem? What tasks can be solved jointly? How to trade off the efficiency and model complexity?

2. *HC*-Nets Learning for Variable Length Sequences.

How to form a fixed length representation for the non-fixed length input-output pair?

Variable Length Input (e.g., sentence)

(Fixed Length Representation)

3. Joint Learning of *H* and *C* networks in *HC*-Nets.

Stage-wise training does not follow the end-to-end learning principle.



Publications



• Prune-and-Score: Learning for Greedy Coreference Resolution.

Chao Ma, Janardhan Rao Doppa, Xiaoli Fern, Tom Dietterich, and Prasad Tadepalli. Proceedings of International Conference on Empirical Methods in Natural Language Processing (EMNLP), 2014.

• Multi-Task Structured Prediction for Entity Analysis: Searchbased Learning Algorithms.

Chao Ma, Janardhan Rao Doppa, Prasad Tadepalli, Hamed Shahbazh, and Xiaoli Fern. Journal of Machine Learning Research (JMLR), Proceedings Track, Vol 77, 16 pages, 2017.

Randomized Greedy Search for Structured Prediction: Amortized Inference and Learning

Chao Ma, F A Rezaur Rahman Chowdhury, Aryan Deshwal, Md Rakibul Islam, Janardhan Rao Doppa, and Dan Roth. Proceedings of International Joint Conference on Artificial Intelligence (IJCAI), 2019.



Thank you! Questions







Structured Prediction with Deep Neural Networks

Papers



- Structured Prediction Energy Networks (ICML16)
- End-to-End Learning for Structured Prediction Energy Networks (ICML17)
- Learning Approximate Inference Networks for Structured Prediction (ICRL18)
- Deep Structured Prediction with Nonlinear Output Transformations
 (NIPS18)
- Deep Value Networks Learn to Evaluate and Iteratively Refine Structured Outputs (ICML17)
- Gradient-based Inference for Networks with Output Constraints (AAAI19)

Structured Prediction Energy Networks (SPEN)



David Belanger, Andrew McCallum

- Formulating the output as a binary vector $y \in \{0, 1\}^{T}$, then relax y to 1. real value space so that $\tilde{y} \in [0, 1]^{T}$.
- Define an energy network E(x, y) to scoring a given pair of input x and 2. output y.
- To do inference for a given input x, the best y can be found by compute 3. *argmin_y E*(x,y). *argmin* is done by doing gradient descent in the relax output space.
- Learning of *E* optimizes a SSVM style loss, with inner-loop loss-4. augmented inference.

Formulating the output as a binary vector $y \in \{0, 1\}^T$, then relax y to real value space so that $\tilde{y} \in [0, 1]^T$.

A output of traditional NN for classification:



y: concatenation of *T* one-hot vectors



 $\hat{y} = \operatorname{argm} in_y E(x, y)$. argmin is done by doing gradient descent in the relax y space.

Manually:

Define a step_size η and number-of-steps T, and an initial output y_0 At each step, update output by doing following:

$$\mathbf{y}_T = \mathbf{y}_0 - \sum_{t=1}^T \eta_t \frac{d}{d\mathbf{y}} E_{\mathbf{x}}(\mathbf{y}_t).$$

Automatically:

Use the GradientDescent optimizer from the library to finish the task above.

Note: After got the real value \tilde{y} , a threshold value should be decided through validation set to round it back to discrete space.



Energy network learning in SPEN



• SPEN relies on a good initial weight. It usually requires a pretraining with a light-weighted network



- The outputs during inference are not exploited.
- The gradient based inference requires a lot of parameters.
- Requires pretraining to initialize the network weights.



End-to-End SPEN



Three improvement over the original SPEN:

1. Improve unstable problem of gradient based inference.

Instead, we have found it useful to avoid constrained optimization entirely, by optimizing un-normalized logits \mathbf{l}_t , with $\mathbf{y}_t = \text{SoftMax}(\mathbf{l}_t)$:

 $\mathbf{l}_{t+1} = \mathbf{l}_t - \eta_t \nabla E_{\mathbf{x}} \left(\text{SoftMax}(\mathbf{l}_t) \right).$ (8)

- 2. Improve the gradient based inference to converge faster.
 - Maintain the same optimization configuration, such as T, at both train and test time.
 - Exploit all the outputs of each iterate to do the update $L = \frac{1}{T} \sum_{t=1}^{T} w_t \ell(\mathbf{y}_t, \mathbf{y}^*)$, where the w could be $w_t = \frac{1}{T-t+1}$ in practice.
 - Set T to a small value.
- 3. Examples of applying SPEN on different tasks.

Inference Network for SPEN



Instead of gradient based inference, another method to compute $\operatorname{argm}_{y}^{y} E(x, y)$ for SPEN: learning another inference network A(x) that can directly generate an output y.

$$\mathbf{A}_{\Psi}(\boldsymbol{x}) \approx \operatorname*{argmin}_{\boldsymbol{y} \in \mathcal{Y}_{R}(\boldsymbol{x})} E_{\Theta}(\boldsymbol{x}, \boldsymbol{y})$$

Learning of Inference network:

$$\hat{\Psi} \leftarrow \operatorname*{argmin}_{\Psi} \sum_{\boldsymbol{x} \in X} E_{\Theta}(\boldsymbol{x}, \mathbf{A}_{\Psi}(\boldsymbol{x}))$$

Learning of inference network and energy network:

$$\min_{\Theta} \max_{\Phi} \sum_{\langle \boldsymbol{x}_i, \boldsymbol{y}_i \rangle \in \mathcal{D}} \left[\triangle (\mathbf{A}_{\Phi}(\boldsymbol{x}_i), \boldsymbol{y}_i) - E_{\Theta}(\boldsymbol{x}_i, \mathbf{A}_{\Phi}(\boldsymbol{x}_i)) + E_{\Theta}(\boldsymbol{x}_i, \boldsymbol{y}_i) \right]_{+}$$
Loss-augmented inference network A_{Φ} can not be directly used as A_{Ψ} in testing. Needs additional training by initializing A_{Φ} with A_{Ψ} weight once E is fixed.

Inference Network for SPEN



Form of inference network A(x)

The architecture of A_{Ψ} will depend on the task.

- For MLC, they use a feed-forward network for A_{Ψ} with a vector output, treating each dimension as the prediction for a single label.
- For sequence labeling, they use an RNN that returns a vector at each position of *x*. We interpret this vector as a probability distribution over output labels at that position.

There is an analogy here to the discriminator in GANs. The energy function is updated so as to enable it to distinguish "fake" outputs produced by A_{\emptyset} from real outputs y_i

Deep Value Networks (DVN)



Michael Gygli, Mohammad Norouzi, Anelia Angelova

- Learning a value network v(x, y) to scoring input output pair such that v can imitate the function of $v^* = 1 l(x, y, y^*)$.
- Inference is done with the similar approach as SPEN: output space gradient descent.
- The learning of v contains two critical step: Generating output for each input, and optimize the cross-entropy loss between v and v* given all (x, y) pairs in each mini-batch.

Difference between DVN and SPEN:

- For SPEN, the absolute energy value is not important, but for DVN, the absolute value matters.
- DVN is optimizing continuous cross-entropy loss between v and v*, while SPEN is optimizing SSVN style hinge loss.

Deep Value Networks (DVN)



Potential problems of DVN:

1. DVN learns more that what is really needed. The absolute predicted value is unnecessary because during inference you will come across a very small proportion of outputs, rather the whole solution space. For some structured output, coming up a fixed length representation might be difficult.

2. DVN learning performance is very sensitive to what outputs that are generated during training.

3. In practice, the gradient based inference in DVN shows a very critical issue: it has no idea *where to stop*.

One has to carefully choose the parameters of inference: number of steps, and step_size, threshold for rounding, etc.
Deep Value Networks (DVN)



Potential problems of DVN:

2. In practice, the gradient based inference in DVN shows a very critical issue: it has no idea *where to stop*.

Results of different number-of-steps with DVN and gradient-base inference:

Train with	Test with	Yeast	Bibtex	Bookmarks
Gradient-20-steps	Gradient-20-steps	63.9	44.5	36.6
Gradient-20-steps	Gradient-10-steps	47.8	34.7	31.2
Gradient-20-steps	Gradient-30-steps	60.2	41.3	31.2
Gradient-20-steps	Gradient-40-steps	57.6	37.9	27.8
Gradient-10-steps	Gradient-10-steps	45.5	37.8	-
Gradient-30-steps	Gradient-30-steps	60.6	42.8	-
Gradient-40-steps	Gradient-40-steps	57.9	37.2	-

Table 2: Gradient-based inference testing performances.

Results of performing discrete greedy search given learned DVN value functions:

Algs.	Yeast	Bibtex	Bookmarks
Search-2-steps	56.3	41.5	34.9
Search-3-steps	59.6	39.5	35.1
Search-4-steps	61.1	35.7	30.4
Search-5-steps	63.4	32.3	27.6
Search-6-steps	62.2	29.1	23.1

 Table 3: Multi-label classification F1 performance.

Single Task Structure Prediction



Typical (Single-Task) Structured Prediction:



Search Based Inference for MTSP

Oregon State

<u>Complete Output</u> Search Space:

- State: y A complete structural output e.g.: a document with 5 mentions, $y_{ner} = (ORG, PER, PER, LOC, VEL)$
- Action: $a = (i, v_j, v_k)$ Change the value of *i* th variable from v_j to v_k e.g.: (ORG, PER, PER, LOC, VEL) a = (2, PER, ORG) (ORG, ORG PER, LOC, VEL) Execute action
- Successor Function: A(y) Set of all possible child states of y Assume T = |y|, and d is domain size, then |A(y)| = (d-1)T
- Initial State: \mathcal{Y}_0 Random output or prediction output of unary classifier. e.g.: use a *multi-class classifier* to predict a label on each mention, and use these predictions as initial output
- Terminal State: \hat{y} An output that reaches local optimal cost

With respect to the outputs in **beam** and all **successor** outputs

Partial vs. Complete Output Space



Partial

Advantage:

Branching factor is small. Greedy search can be very fast. Explicit initial and terminal state.

Limitation:

Can be overcome with **beam**:

i.e., LaSO, seq2seq-BSO Requires an ordering. Value function (ground truth) supervision is only local oracle.

LSTMs or GRUs with Attention VS.

Complete

Advantage:

All the disadvantages of Partial space can be overcome.

Limitation:

Requires initial states, and not explicit terminal state. Computational expensive on both time and space.